

#### **Fall 2023**

## **WEEK 5 STUDY GUIDE**

# **The Big Picture**

We start by finding probabilities and expectations by conditioning. The next topic is the examination of a random process indexed by time, defined in terms of conditional distributions.

- Conditioning is a great way of finding expectations, just as it is for finding probabilities.
- In many situations involving i.i.d. trials, there is a recursive structure that can be used to simplify

calculations.

- A *stochastic process* is a random process indexed by time. A Markov chain is a stochastic process with a particular dependence structure that allows it to be used as a simple model in many settings.
- Markov chains run for a long time have very interesting and useful properties.

## **Week At a Glance**

Mon 9/18	Tue 9/19	Wed 9/20	Thu 9/21	Fri 9/22
	Lecture	Sections	Lecture	Mega Sections
HW 4 Due HW 5 (due NOON Mon 9/25)				Practice Midterm Walk-through 2-4PM
Lab 3A Due Lab 3B (due NOON Mon 9/25)			Lab 3B party 10AM - noon	
Skim Sec 9.1 and 9.2	Work through Chapter 9	Take a break, or skim Ch 10.1 if you want to	Work through Ch 9.	Finish assignments.

# **Reading, Practice, and Class Meetings**

Book	Topic	Lectures: Instructors	Sections: TAs	Optional Additional Practice
Ch 9	Expectation by conditioning  - 9.1 is the old multiplication rule combined with recursion, to find probabilities quickly - 9.2 shows how to find expectation by conditioning, building on the familiar calculation of finding an overall average as a weighted average of group averages - 9.3 has examples in the context of i.i.d. Bernoulli trials	Tuesday 9/19 - Probabilities and expectation by conditioning and recursion	Wednesday 9/20 - Ch 9 Ex 1, 2, 4	All Chapter 9 Exercises not covered in sections. Some are clones of homework problems.
Ch 10	Markov chains  - 10.1 introduces terminology, notation, and basics, along with a computational approach to the long run - 10.2 narrows down the type of chain we'll be studying, but even the narrowed-down group is pretty large - 10.3 takes a more theoretical approach to the long run - 10.4 has examples and applications	Thursday 9/21  - Introduction to Markov chains - Long run behavior	Friday 9/22 - Ch 9 Ex 5 - Some midterm practice	None. There are no exercises in Ch 10. All the Markov Chains exercises are in Ch 11, at which point you'll have techniques that make some of the solutions easier.